PLEASURE TEST REVISION SERIES By: OP GUPTA (+91-9650 350 480)

SUBJECT – MATHEMATICS FOR CLASS XII

Time Allowed: 180 Minutes

Max. Marks: 100 [SECTION – A] **Q01.** Let * be a binary operation defined by a*b = 2a + b - 3, find the value of 3*4. **Q03.** What is the value of Δ , if $\Delta = \begin{vmatrix} a + ib & c + id \\ -c + id & a - ib \end{vmatrix}$? **Q02.** Write the value of: $\sin^{-1} \left(\sin \frac{3\pi}{5} \right)$. **Q04.** Check if the function $-\frac{x^3}{3} + x^2 - x + \frac{3}{2}$ is decreasing in R. **Q05.** For what value of 'm' and 'p', is the matrix $\begin{pmatrix} 0 & 5 & -3 \\ -5 & m & 4 \\ n & -4 & 0 \end{pmatrix}$ skew-symmetric? **Q06.** Show that a powerful bomb shot along the line of fire $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$ will never hit a helicopter flying in the plane 2x + 4y - 4z + 11 = 0. **Q07.** Write the number of binary operations that can be defined on the set $\{1, 2\}$. Q08. Let \vec{a} and \vec{b} are non-collinear vectors. For what value of x, the vectors $\vec{c} = (x-2)\vec{a} + \vec{b}$ and $\vec{d} = (2x+1)\vec{a} - \vec{b}$ are collinear? **Q09.** Write a unit vector perpendicular to the vectors \vec{a} and \vec{b} both, if it is given that $\vec{a} = 3\hat{i} + 2\hat{j} + 6\hat{k}$ and **Q10.** Evaluate: $\int \frac{3\cos x}{2\sin^2 x} dx$. $\vec{b} = \hat{i} + 2\hat{j} + 2\hat{k}$. [SECTION – B] 1 - x, if x < 1**Q11.** Discuss the differentiability of f (x) = $\left\{ (1-x)(2-x), \text{ if } 1 \le x \le 2 \text{ at } x = 2. \right\}$ 3 - x, if x > 2(OR) A car driver is driving a car on the dangerous path given by $f(x) = \begin{cases} \frac{1-x^{m}}{1-x}, & \text{if } x \neq 1 \\ 1-x, & \text{m} \in N. \end{cases}$ m - 1, if x = 1Find the dangerous point (point of discontinuity) on the path. Whether the driver should pass that point or not? Justify your answer. **Q12.** Let $\vec{a} = 2\hat{i} + \hat{k}$, $\vec{b} = \hat{i} + \hat{j} + \hat{k}$ and $\vec{c} = 4\hat{i} - 3\hat{j} + 7\hat{k}$ be three vectors. Determine a vector \vec{r} which satisfies the condition $\vec{r} \times \vec{b} = \vec{c} \times \vec{b}$ and $\vec{r} \cdot \vec{a} = 0$. Q13. Express $\cos^{-1} \sqrt{\frac{\sqrt{1+x^2+1}}{2\sqrt{1+x^2}}}$ in simplest form. (OR) Solve: $\sec^2 \tan^{-1} 2 + \csc^2 \cot^{-1} 3 = x$. **Q14.** Evaluate: $\int_{0}^{\pi} \frac{x \sin x}{1 + \cos^{2} x} dx$. **Q15.** Solve the differential equation: $(x - \tan^{-1} y) dy + (y^{2} + 1) dx = 0$. Q16. If the radius of a sphere is measured as 9 cm with an error of 0.03 cm, then find the approximate error in calculating its volume. (OR) Water is dripping out from a conical funnel at a uniform rate of 4 cm^3 /s through a tiny hole at the vertex in the bottom. When the slant height of the water is 3cm, find the rate of decrease of the slant height of the water-cone. Given that the vertical angle of funnel is 120° . Q17. A chairman is biased so that he selects his relatives for a job 3 times as likely as others. If there are 3 posts for a job, find the probability distribution for selection of persons other than his relatives. If the chairman is biased then, which value of life will be demolished?

Q18. Find the distance of the point (-2, 4, -5) from the line
$$\frac{x+3}{3} = \frac{y-4}{5} = \frac{z+3}{6}$$
.
Q19. Evaluate: $\int \frac{dx}{\sin(x-\alpha)\sin(x-\beta)}$. (OR) Evaluate: $\int \frac{(x+x^3)^{1/3}}{x^4} dx$.
Q20. Let f, g : R \rightarrow R be defined as f (x) = |x| and g (x) = [x], where [x] denotes greatest integer less than or equal to x. Evaluate: $\frac{(gof)\left(-\frac{5}{3}\right) - (fog)\left(-\frac{5}{3}\right)}{(fo(gof))\left(-\frac{5}{3}\right)}$. Q21. If $y^2 = 4ax$, then evaluate: $\left(\frac{d^2y}{dx^2}\right) \cdot \left(\frac{d^2x}{dy^2}\right)$.
Q22. Using properties of determinants, prove that: $\begin{vmatrix} 2bc-a^2 & c^2 & b^2 \\ c^2 & 2ca-b^2 & a^2 \\ b^2 & a^2 & 2ab-c^2 \end{vmatrix} = (a^3+b^3+c^3-3abc)^2$.
Q23. Find the area bounded by $x^2 + y^2 = 25$, $4y = |4-x^2|$, $x = 0$, $y = 0$ which is lying above x-axis.

× 1 2

-- 1

- 0

Q24. Three friends A, B and C visited a Super Market for purchasing fresh fruits. A purchased 1kg apples, 3kg grapes and 4kg oranges and paid ₹800. B purchased 2kg apples, 1kg grapes and 2kg oranges and paid ₹500. While C paid ₹700 for 5kg apples, 1kg grapes and 1kg oranges. Find the cost of each fruit per kg by using matrix method. Why are the fruits good for health?

1

0

-1 0

1

2

- Using elementary operations, find the inverse of 2 3 4 , if it exists. (OR)
- Q25. A manufacturer has three machine operators A (skilled), B (semi-skilled) and C (non-skilled). The first operator A produces 1% defective items whereas the other two operators B and C produce 5% and 7% defective items respectively. A is on the job for 50% of time, B in the job for 30% of the time and C is on the job for 20 % of the time. A defective item is produced, what is the probability that it was produced by B? What is the value of skill in industries?
- Q26. A bird at A(7, 14, 5) in space wants to reach a point P on the plane 2x + 4y - z = 2 when AP is least. Find the position of P and also the distance AP travelled by the bird.
- **Q27.** Evaluate $\int \log \csc x \, dx$, by using properties of the definite integral.
- Q28. Avinash has been given two lists of problems from his mathematics teacher with the instructions to submit not more than 100 of them correctly solved for marks. The problems in the first list are worth 10 marks each and those in the second list are worth 5 marks each. He knows from past experience that he requires on an average of 4 minutes to solve a problem of 10 marks and 2 minutes to solve a problem of 5 marks. He has other subjects to worry about; he cannot devote more than 4 hours to his mathematics assignment. With reference to manage his time in best possible way, how many problems from each list shall he do to maximize his marks? What is the importance of time management for the students?
- If PA and QB be two vertical poles of height 16m and 22m at points A and B respectively such that Q29. AB= 20m then, find the distance of a point R on AB from the point A such that $RP^2 + RQ^2$ is minimum. A point P is given on the circumference of a circle of radius r. The chord QR is parallel to the (OR) tangent line at P. Find the maximum area of the triangle PQR.

Hey, Good Luck For Your Exams.!

Prepared By OP Gupta (+91-9650 350 480) [Electronics & Communications Engineering] Visit at: www.theopqupta.bloqspot.com, www.scribd.com/theopqupta